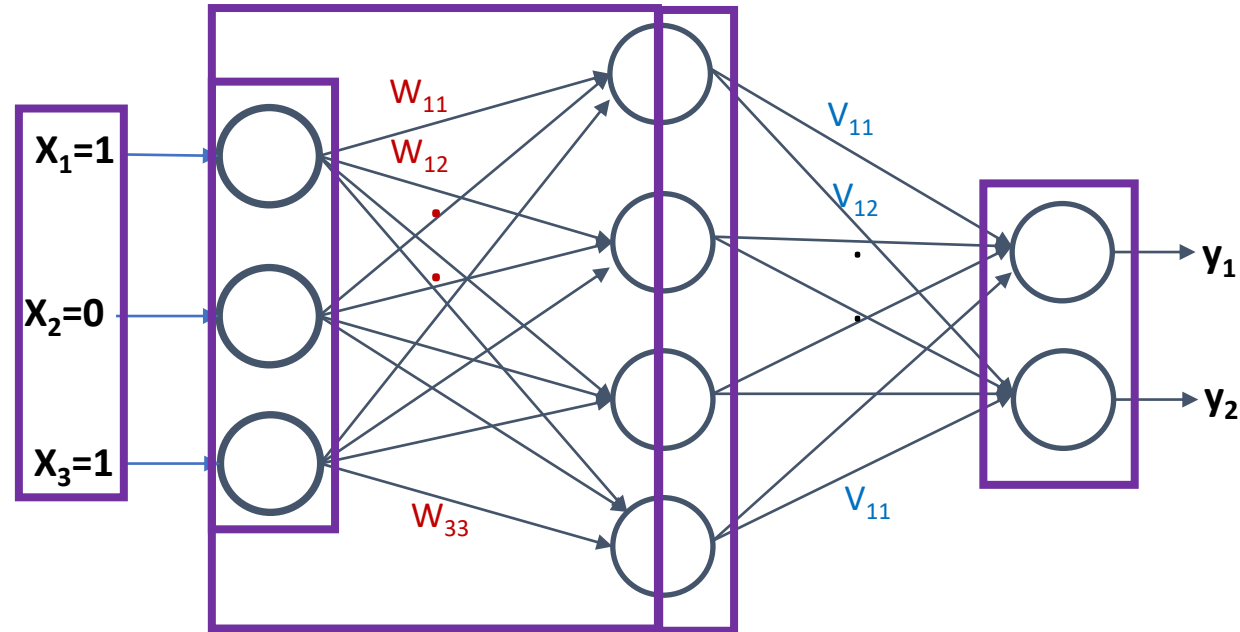


# Lesson 11

Learning the parameters

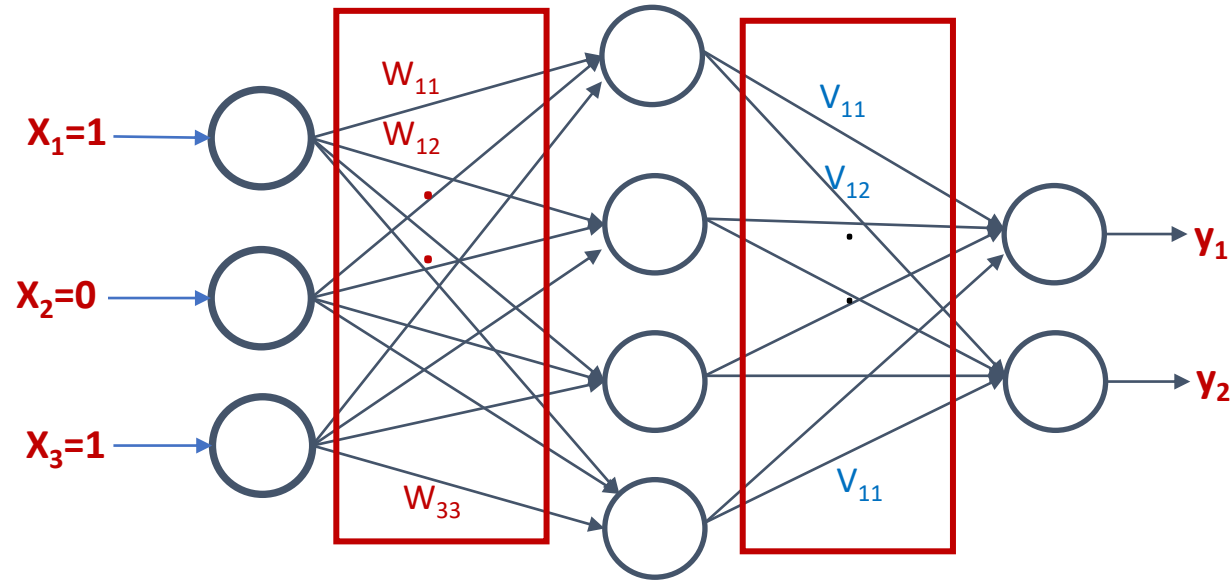
– Backpropagation through time

# What are the parameters?



$$\bar{y}^T = f_{\text{hidden}}(f_{\text{output}}(\bar{x}^T \mathbf{W})^T \cdot \mathbf{V})$$

# What are the parameters?



	$h_1$	$h_2$	$h_3$	$h_4$
$i_1$	$w_{11}$	$w_{12}$	$w_{13}$	$w_{14}$
$i_2$	$w_{21}$	$w_{22}$	$w_{23}$	$w_{24}$
$i_3$	$w_{31}$	$w_{32}$	$w_{33}$	$w_{34}$

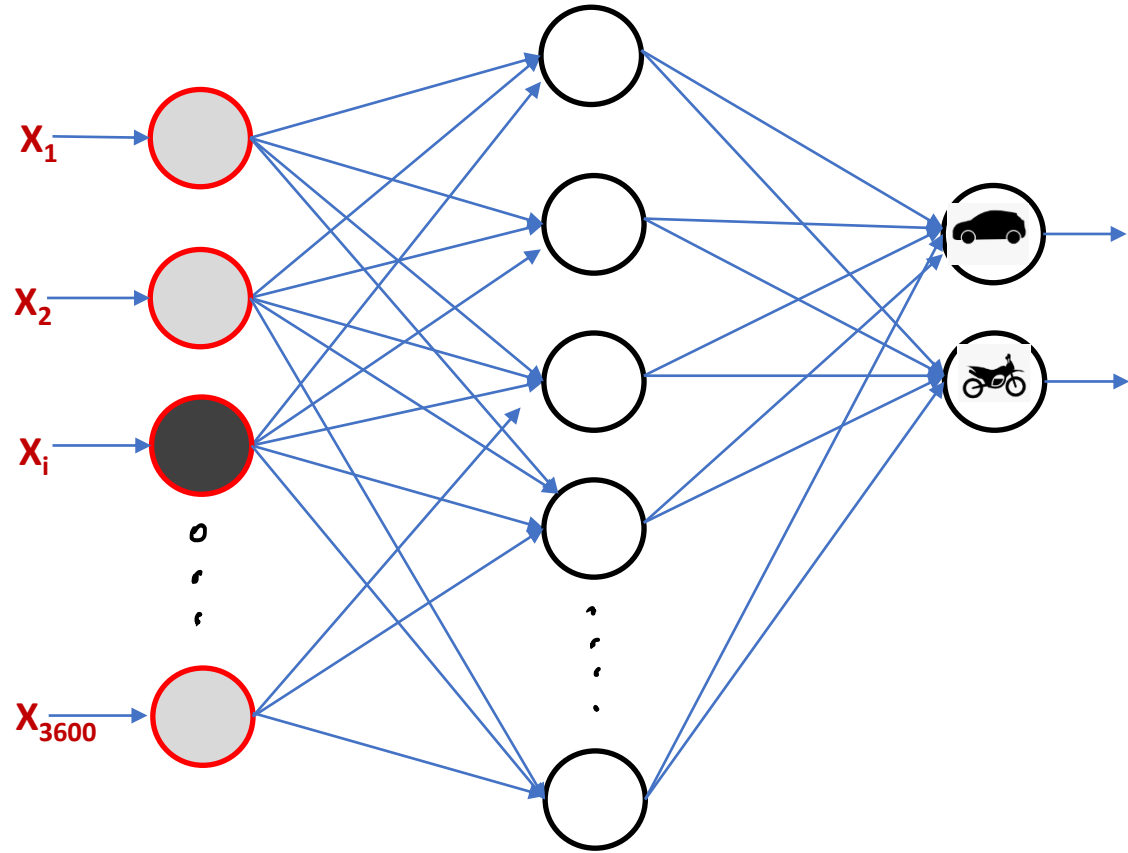
**W**

	$o_1$	$o_2$
$h_1$	$v_{11}$	$v_{12}$
$h_2$	$v_{21}$	$v_{22}$
$h_3$	$v_{31}$	$v_{32}$
$h_4$	$v_{41}$	$v_{42}$

**V**

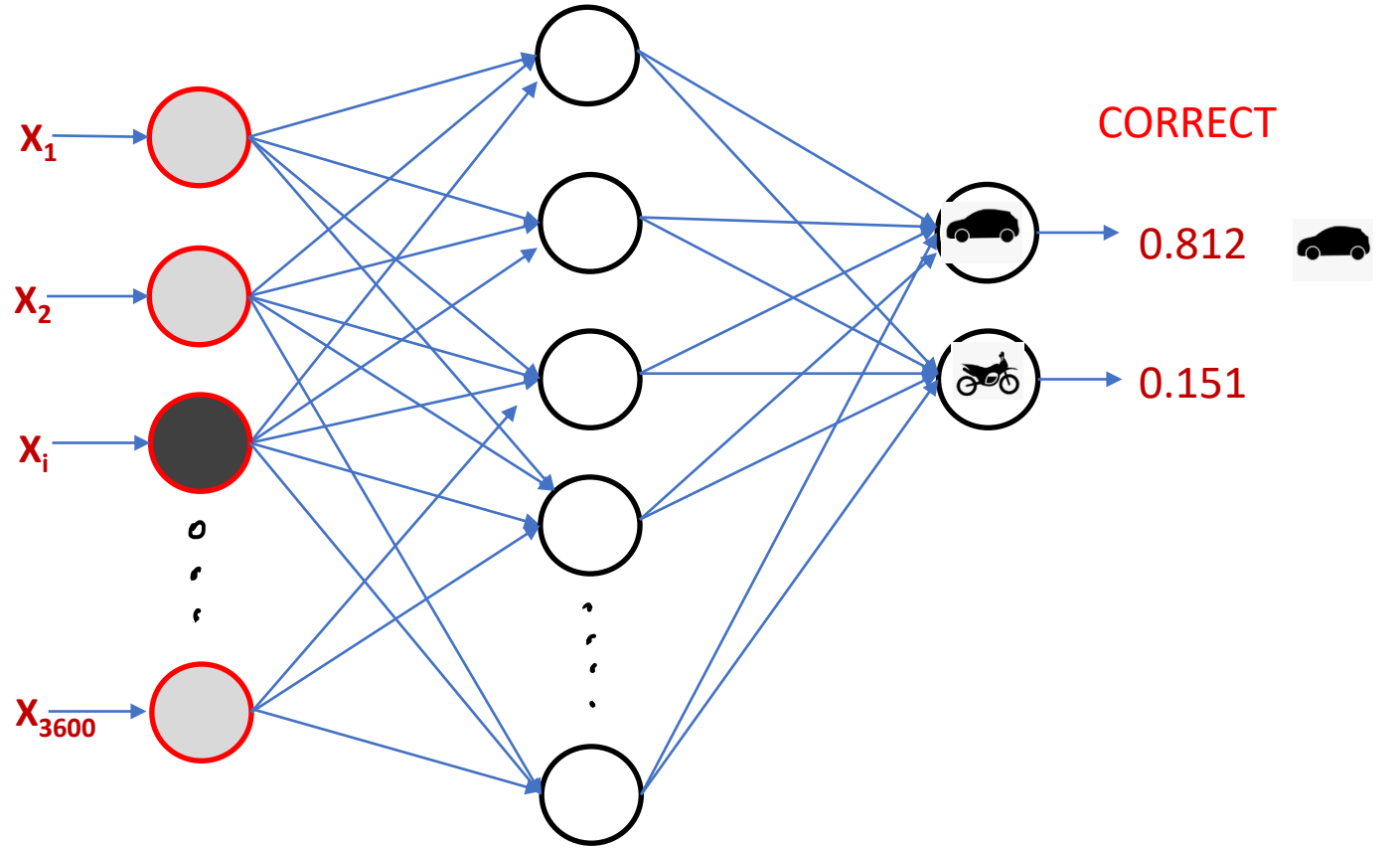


$60 \times 60 = 3600$



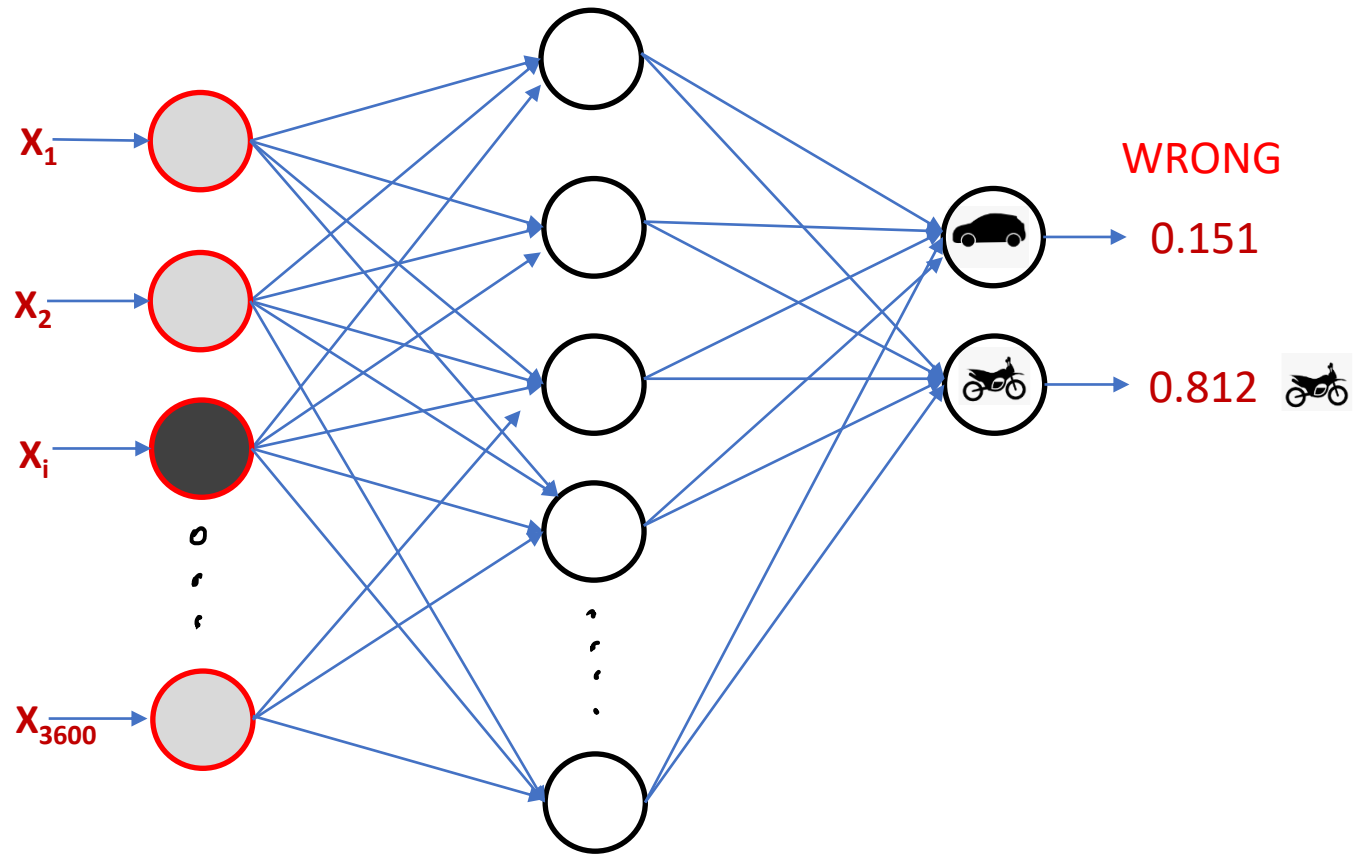


$60 \times 60 = 3600$

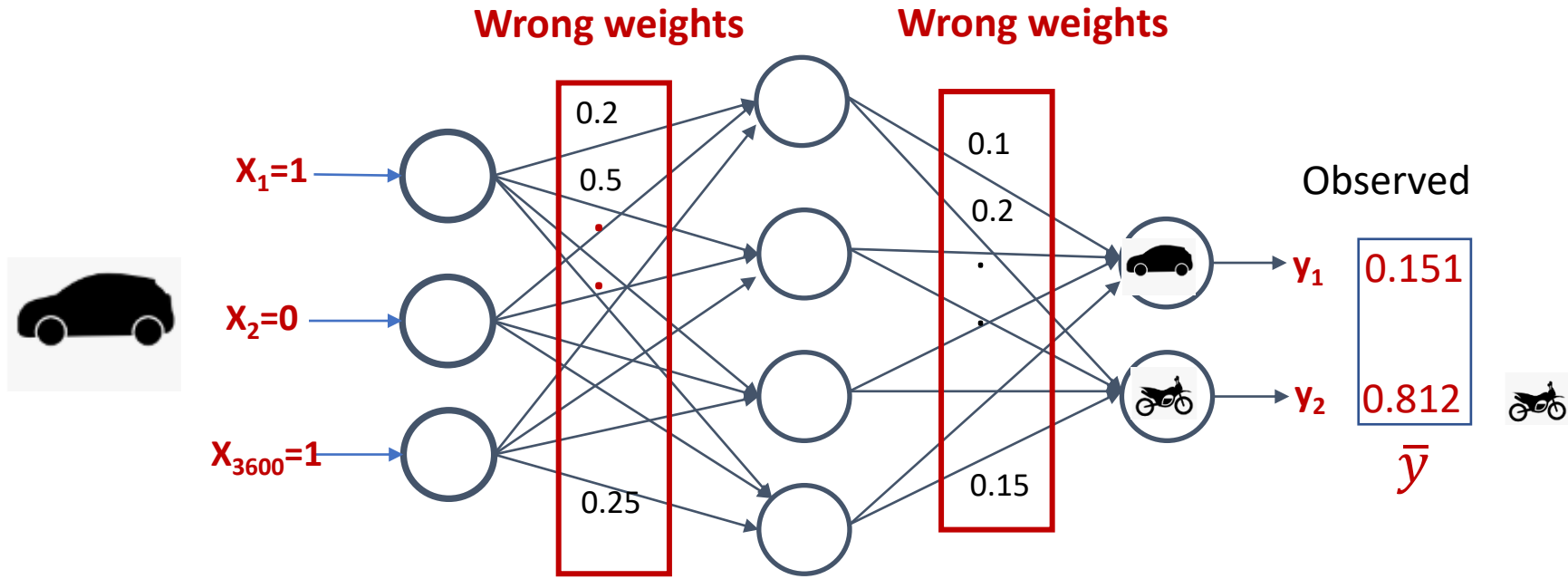




60x60=3600

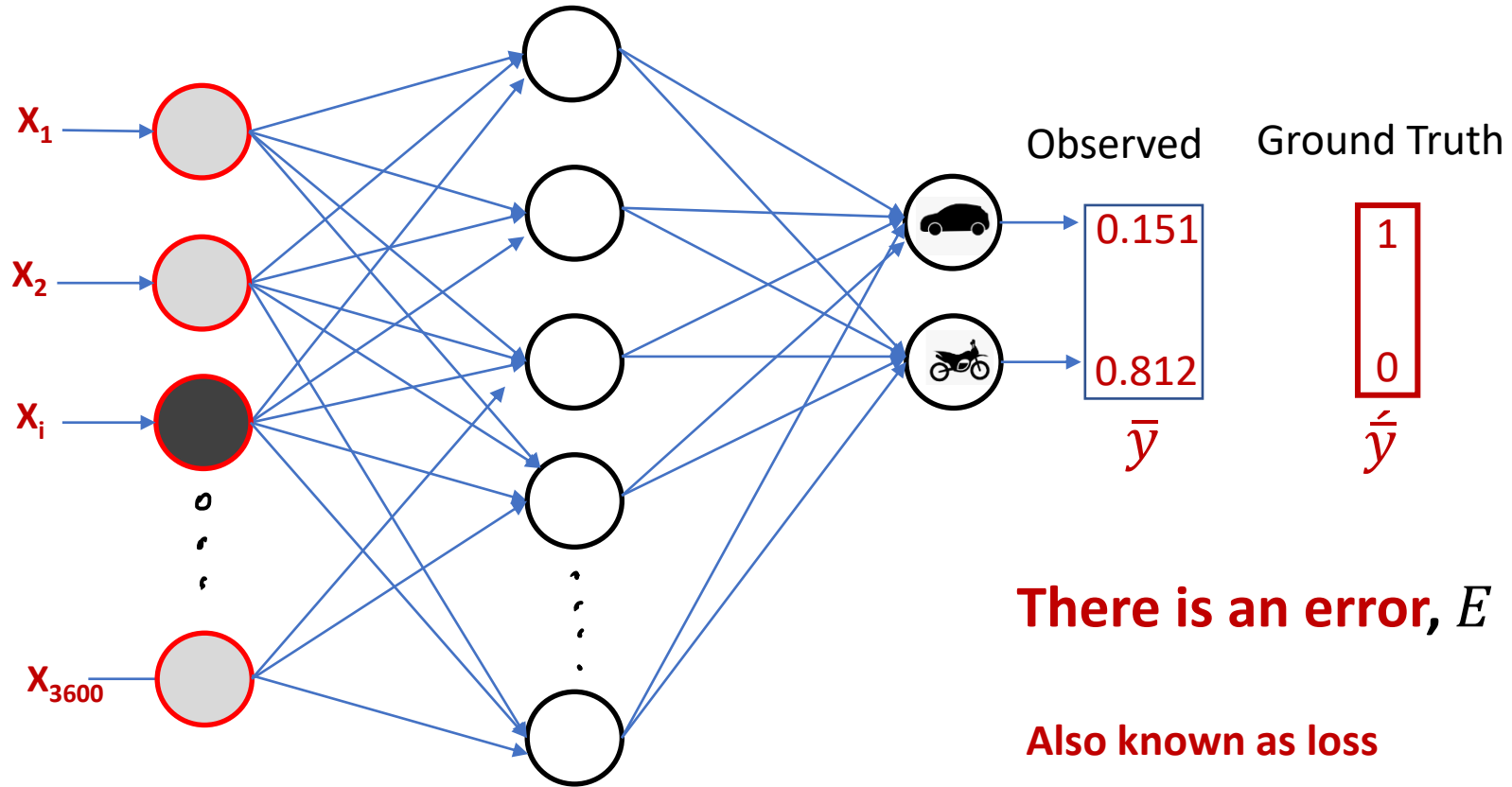


# Why there is an error in prediction?



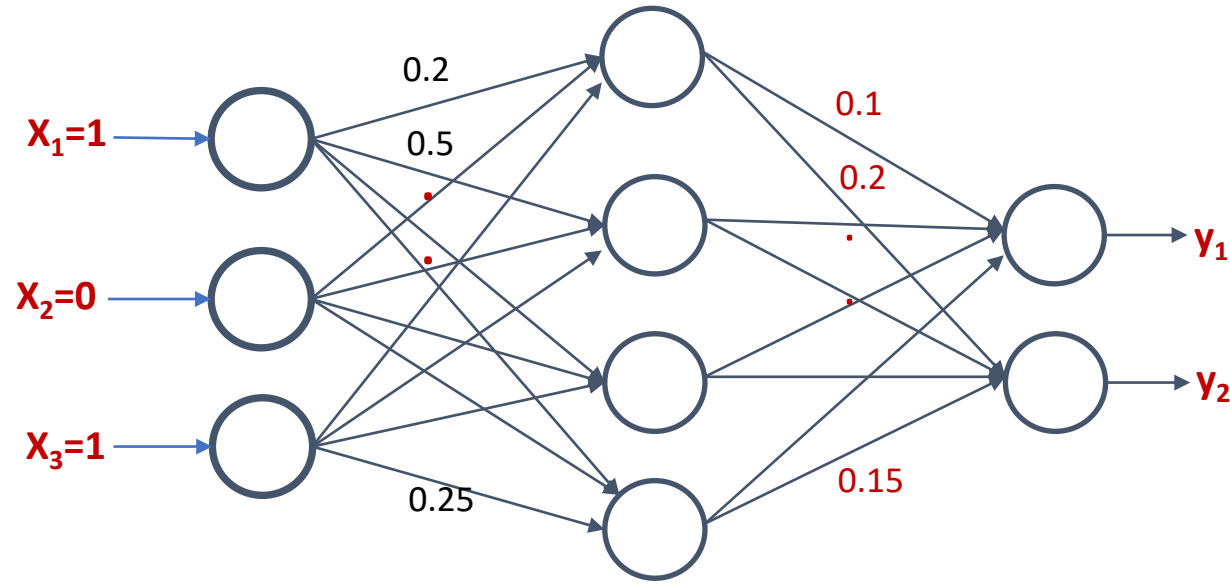


60x60=3600





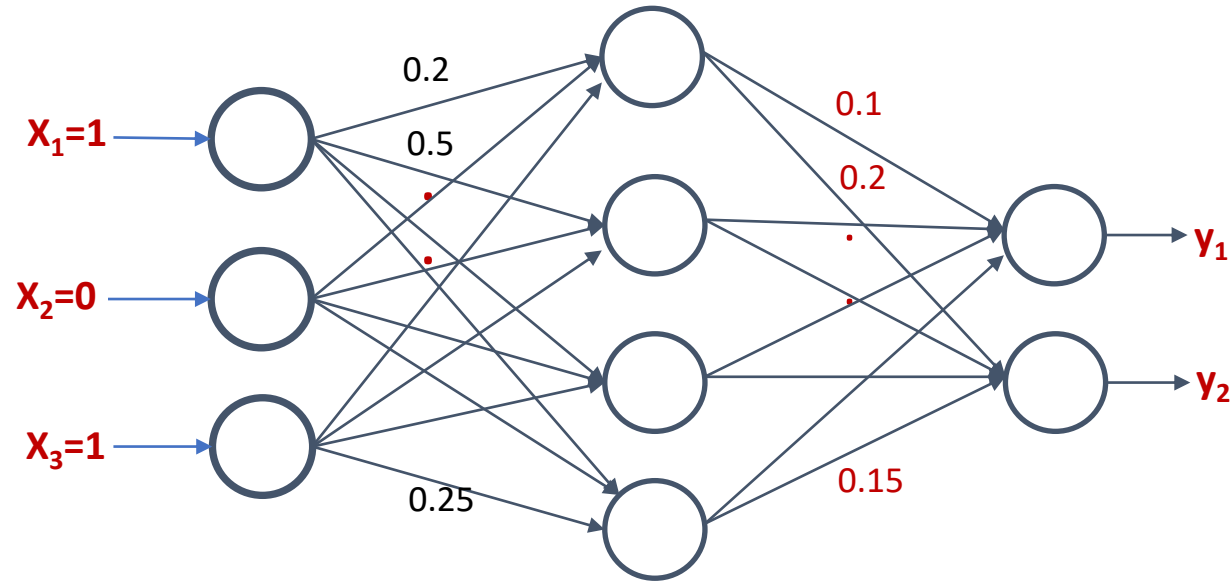
# Backpropagation Through Time



Minimize the Loss function  $E = \|\bar{y} - \hat{y}\|$

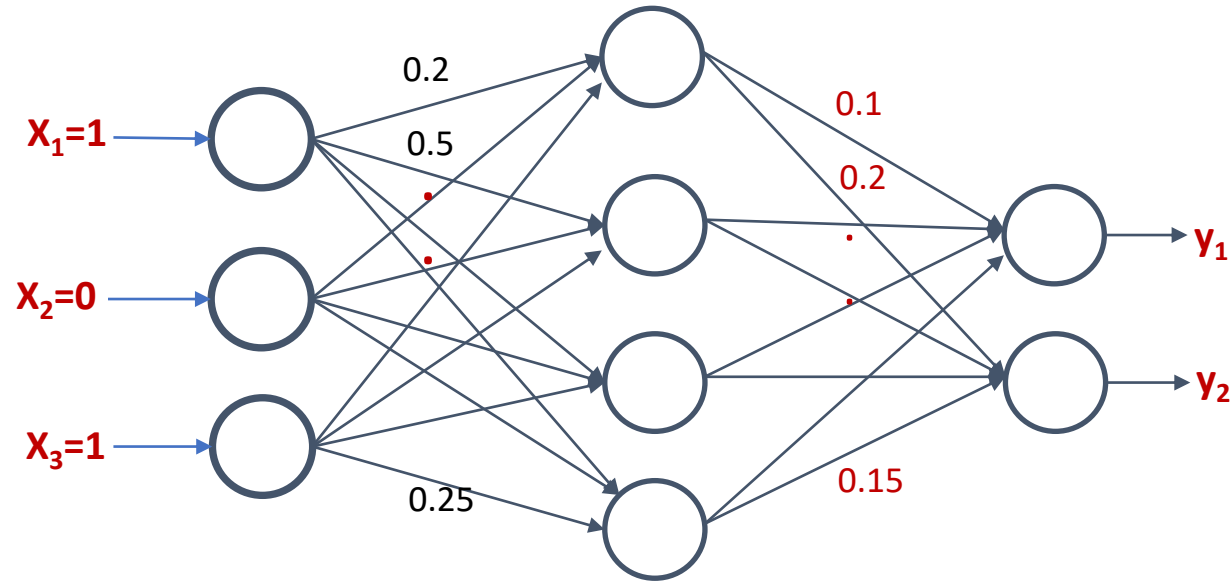
# Backpropagation Through Time

Minimize the Loss function  $E = \|\bar{y} - \hat{y}\|$



# Backpropagation Through Time

Minimize the Loss function  $E = \|\bar{y} - \hat{y}\|$

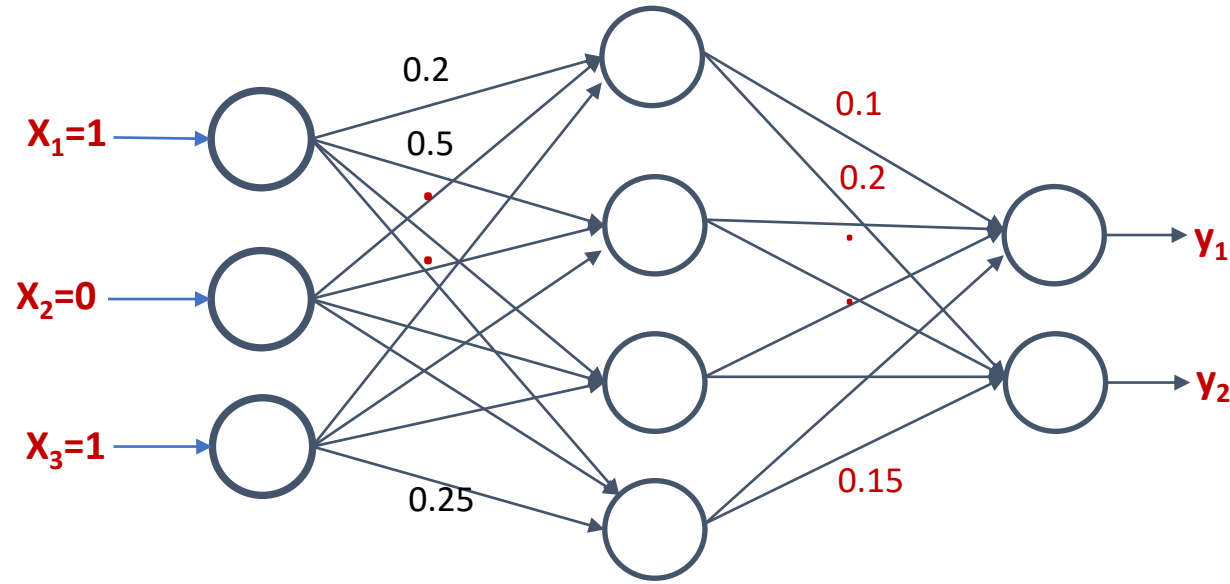


$$\nabla = \frac{\delta E}{\delta V} = 0$$

$$\nabla_{ij} = \frac{\delta E}{\delta V_{ij}} = \frac{\delta \|\bar{y} - \hat{y}\|}{\delta V_{ij}} = 0$$

# Backpropagation Through Time

Minimize the Loss function  $E = \|\bar{y} - \hat{y}\|$



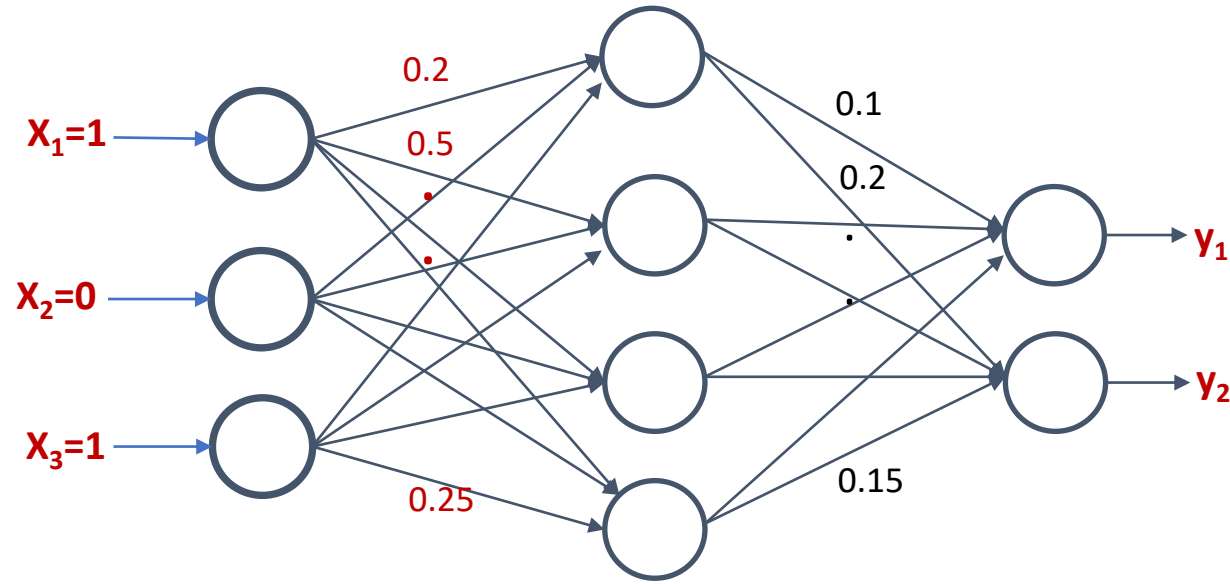
$$\nabla = \frac{\delta E}{\delta V} = 0$$

$$\nabla_{ij} = \frac{\delta E}{\delta V_{ij}} = \frac{\delta \|\bar{y} - \hat{y}\|}{\delta V_{ij}} = 0$$

$$V_{ij}^t = V_{ij}^{t-1} + \eta \nabla_{ij}^t$$

$$\eta = [0, 1]$$

# Backpropagation Through Time

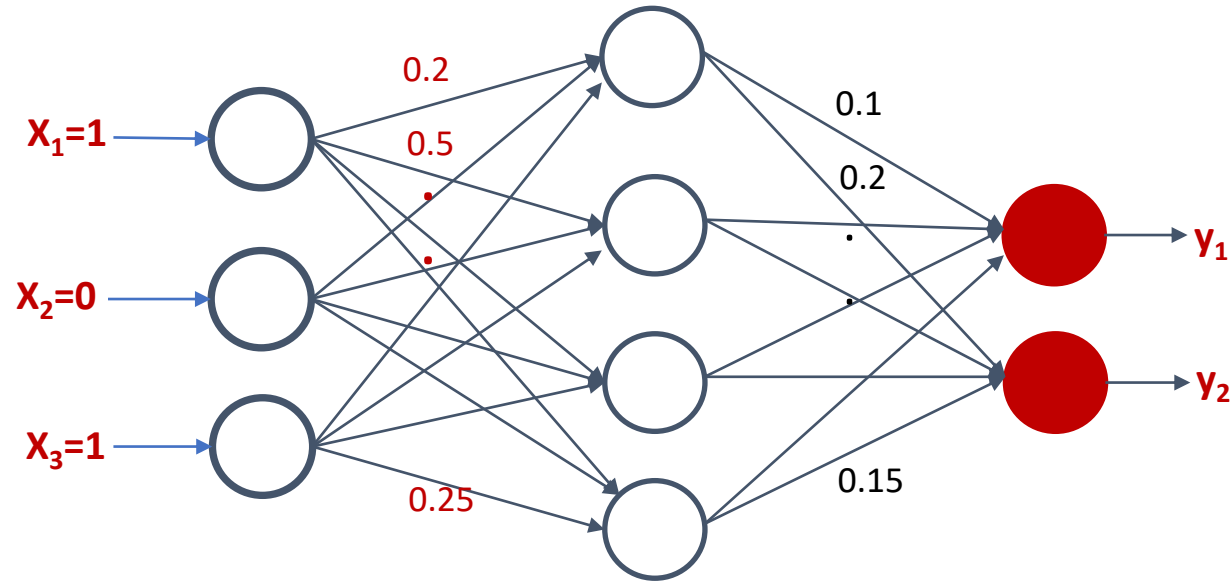


$$E = \|\bar{y} - \hat{y}\| = 0$$

or

$$E = \|\bar{y} - \hat{y}\| \leq \epsilon$$

# Backpropagation Through Time

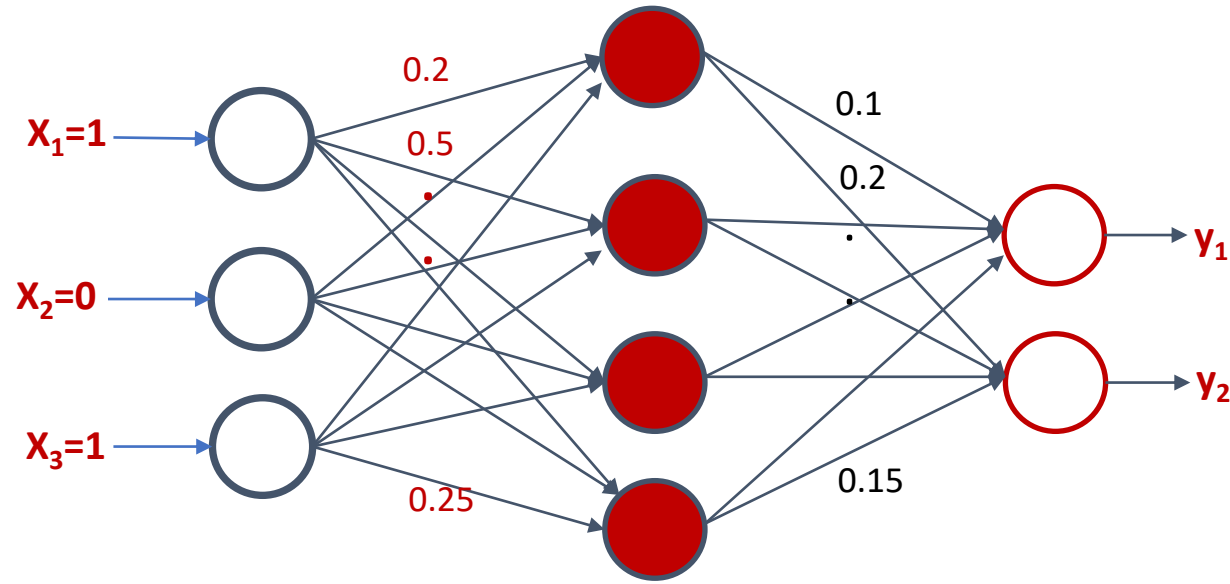


$$E = \|\bar{y} - \hat{y}\| = 0$$

or

$$E = \|\bar{y} - \hat{y}\| \leq \epsilon$$

# Backpropagation Through Time

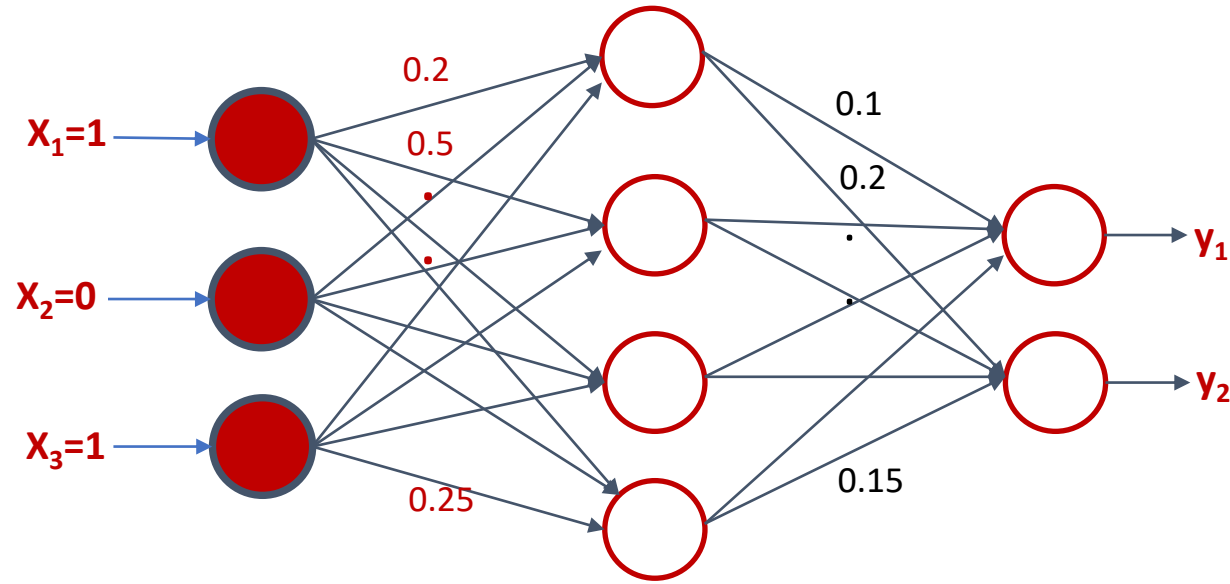


$$E = \|\bar{y} - \hat{y}\| = 0$$

or

$$E = \|\bar{y} - \hat{y}\| \leq \epsilon$$

# Backpropagation Through Time



$$E = \|\bar{y} - \hat{y}\| = 0$$

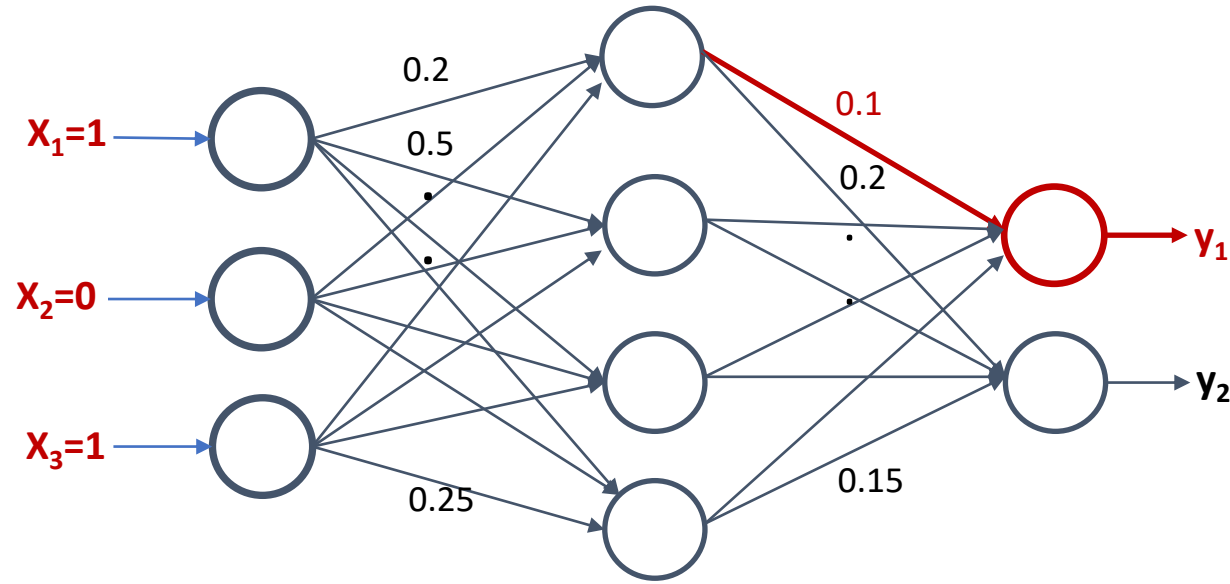
or

$$E = \|\bar{y} - \hat{y}\| \leq \epsilon$$



# How are the Derivatives performed

Loss function  $E = \|\bar{y} - \hat{y}\|$

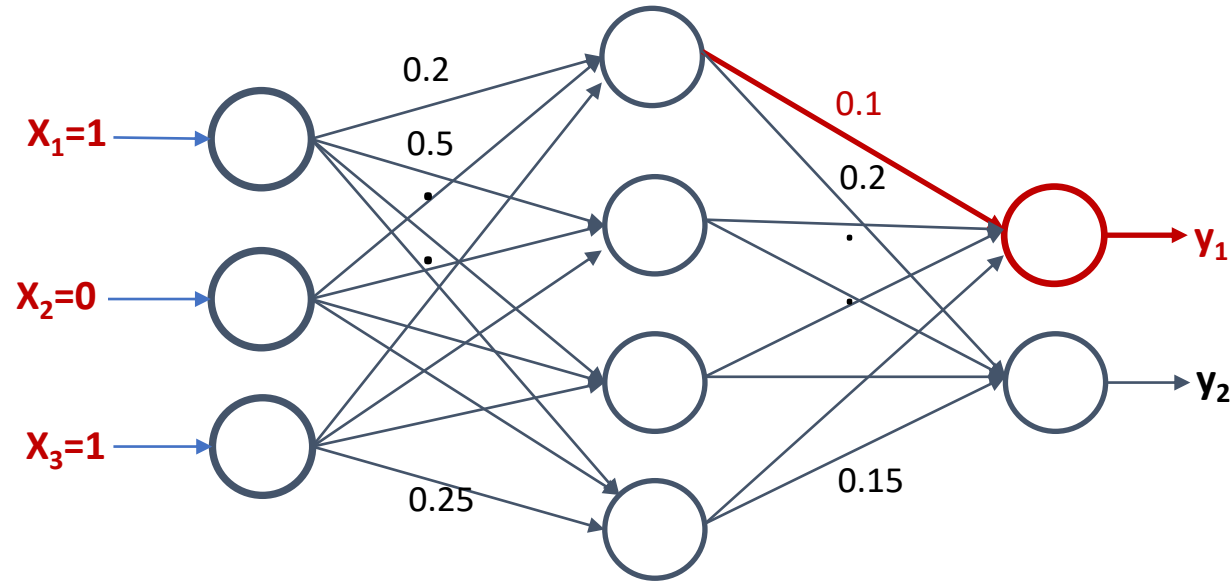


$$\nabla = \frac{\delta E}{\delta V} = 0$$

$$\nabla_{11} = \frac{\delta E}{\delta V_{11}} = 0$$

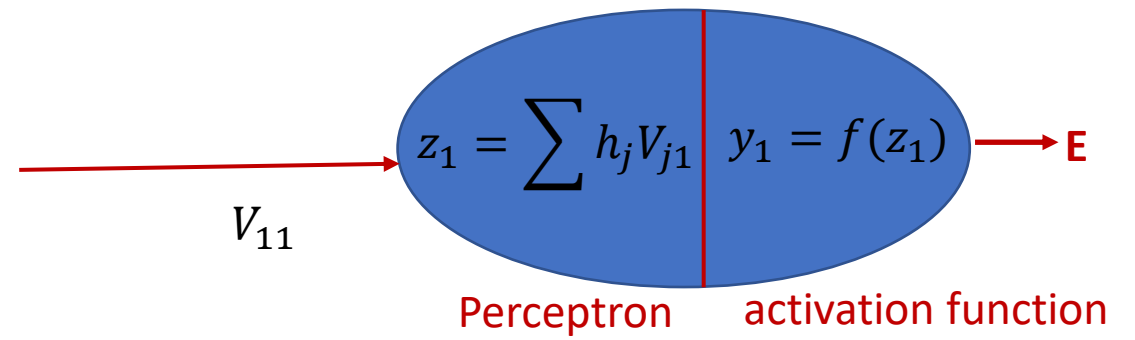
# How are the Derivatives performed

Loss function  $E = \|\bar{y} - \hat{y}\|$



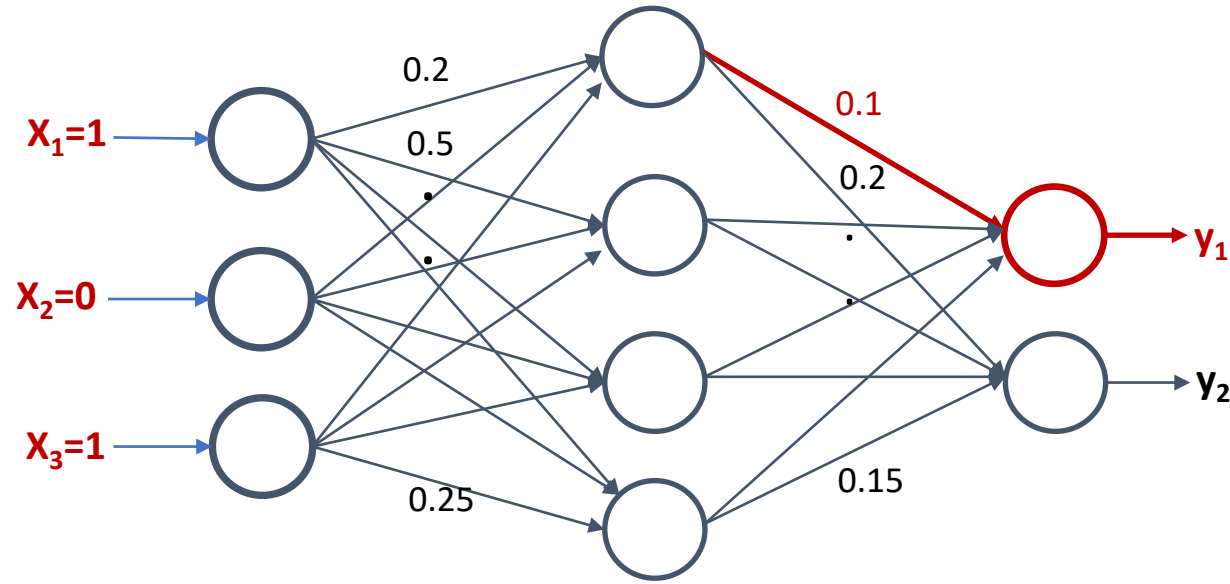
$$\nabla = \frac{\delta E}{\delta V} = 0$$

$$\nabla_{11} = \frac{\delta E}{\delta V_{11}} = 0$$



# How are the Derivatives performed

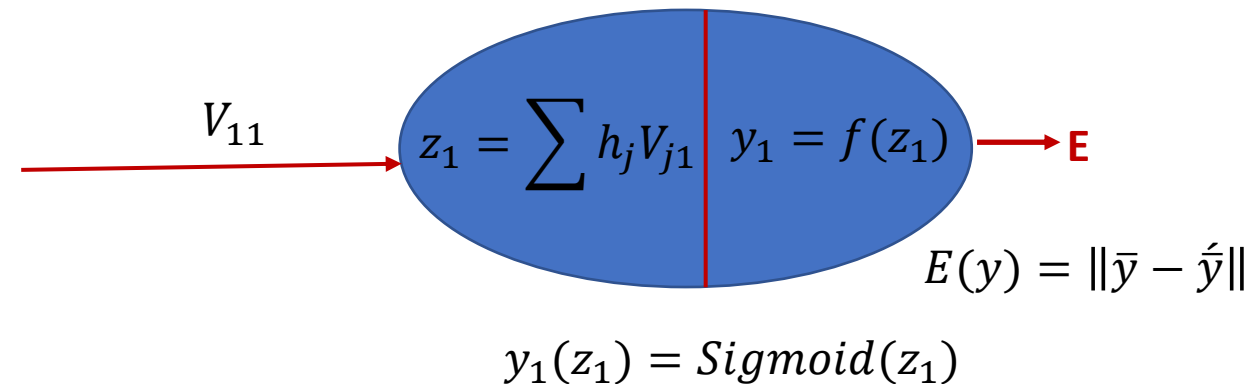
**Loss function**  $E = \|\bar{y} - \hat{y}\|$



$$\nabla = \frac{\delta E}{\delta V} = 0$$

$$\nabla_{11} = \frac{\delta E}{\delta V_{11}} = 0$$

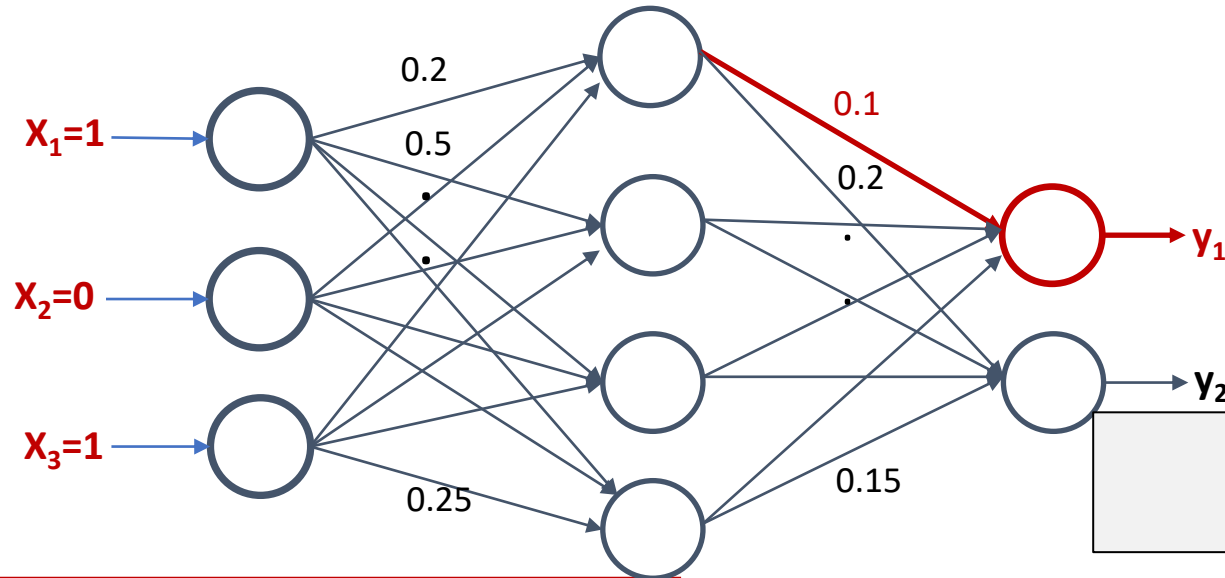
$$z_1(V_{11}) = h_1 V_{11} + h_2 V_{21} + h_3 V_{31} + h_4 V_{41}$$



$$y_1(z_1) = \text{Sigmoid}(z_1)$$

# How are the Derivatives performed

Loss function  $E = \|\bar{y} - \hat{y}\|$



$$\nabla = \frac{\delta E}{\delta V} = 0$$

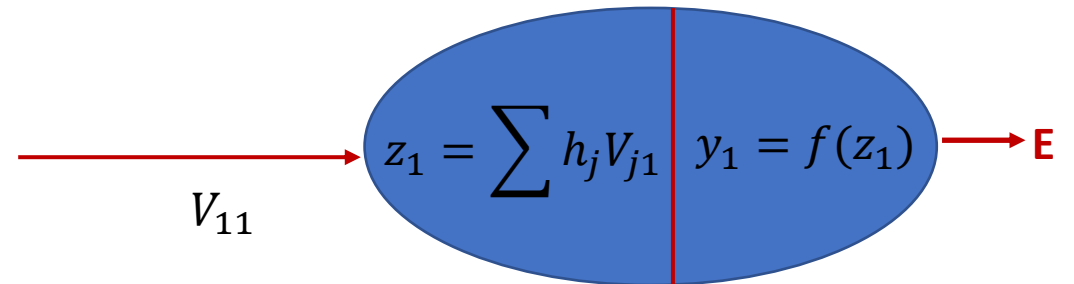
$$\nabla_{ij} = \frac{\delta E}{\delta V_{ij}} = 0$$

$$\frac{\delta E}{\delta V_{11}} = \frac{\delta z_1}{\delta V_{11}} \times \frac{\delta y_1}{\delta z_1} \times \frac{\delta E}{\delta y_1}$$

$$\nabla_{11} = \frac{\delta E}{\delta V_{11}} = \frac{\delta z_1}{\delta V_{11}} \cdot \frac{\delta y_1}{\delta z_1} \cdot \frac{\delta E}{\delta y_1}$$

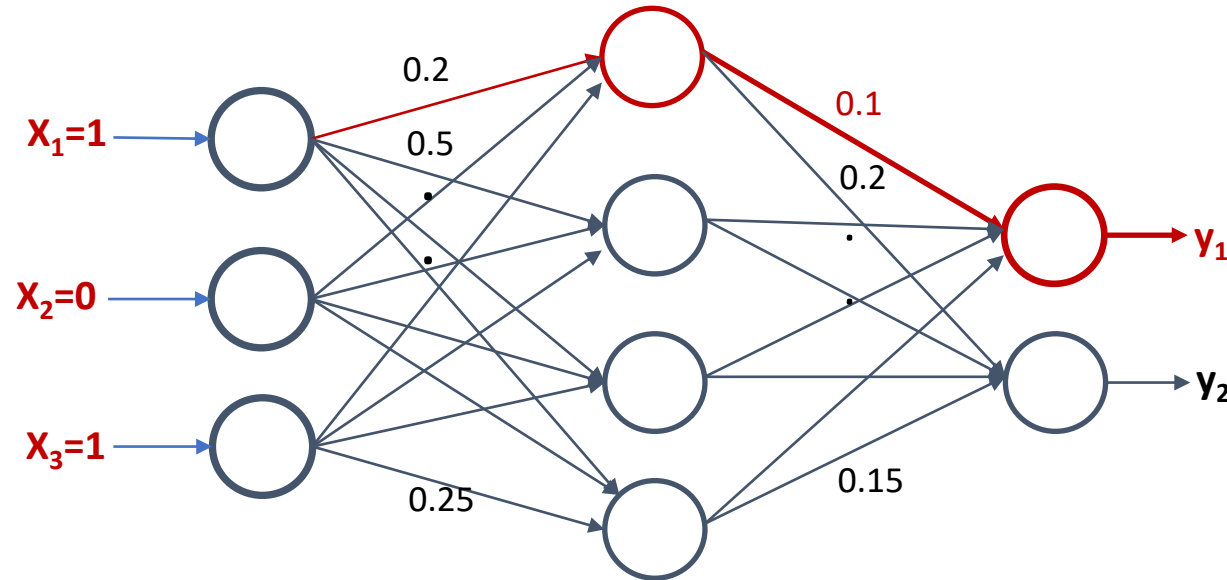
$$z_1 = h_1 V_{11} + h_2 V_{21} + h_3 V_{31} + h_4 V_{41}$$

$$y_1 = \text{Sigmoid}(z_1)$$



# Backpropagation

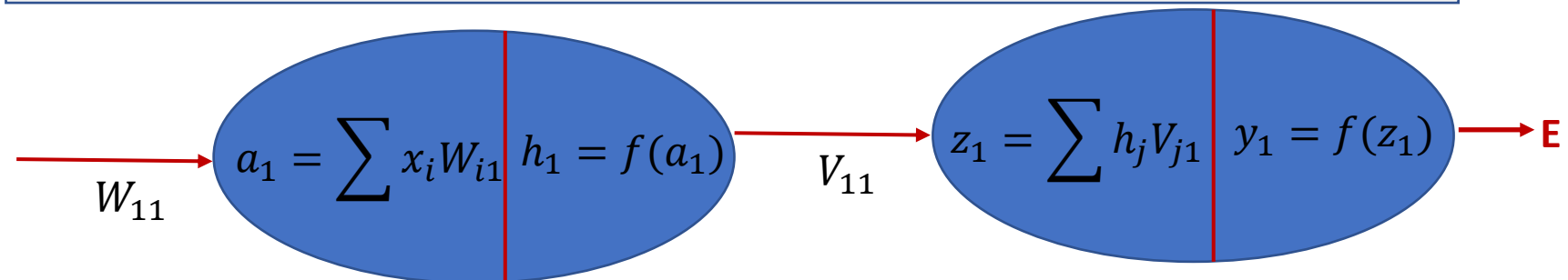
**Loss function**  $E = \|\bar{y} - \hat{y}\|$



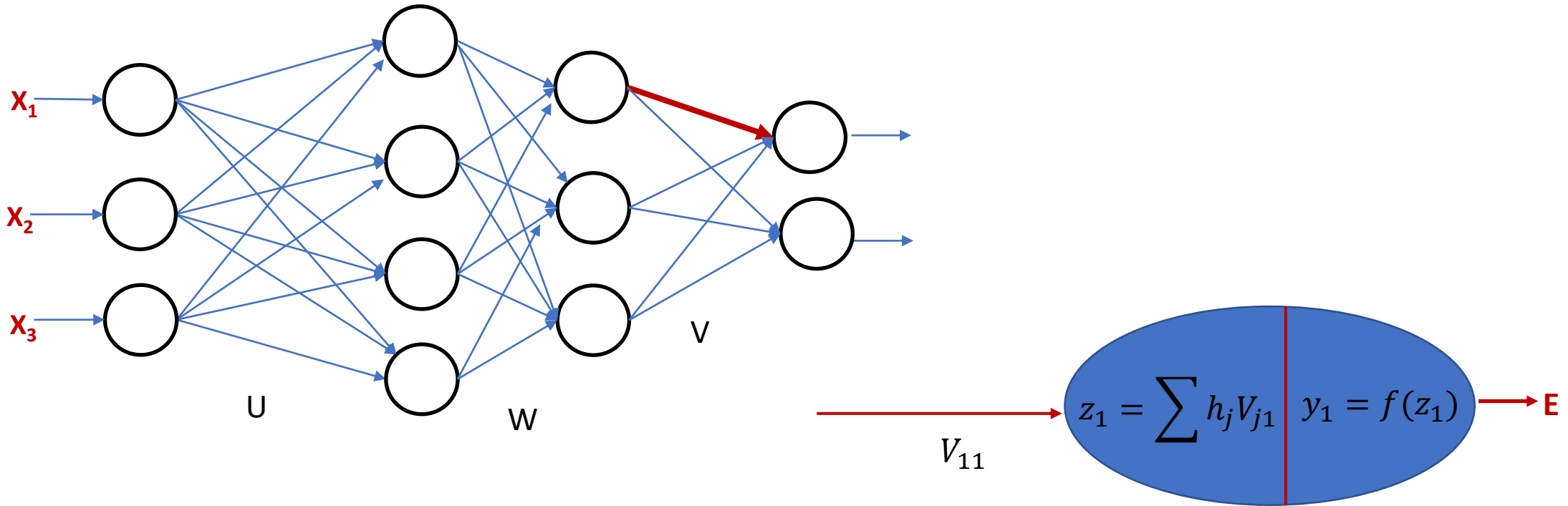
$$\nabla = \frac{\delta E}{\delta W} = 0$$

$$\nabla_{ij} = \frac{\delta E}{\delta W_{ij}} = 0$$

$$\frac{\delta E}{\delta W_{11}} = \frac{\delta a_1}{\delta W_{11}} \times \frac{\delta h_1}{\delta a_1} \times \frac{\delta z_1}{\delta h_1} \times \frac{\delta y_1}{\delta z_1} \times \frac{\delta E}{\delta y_1}$$

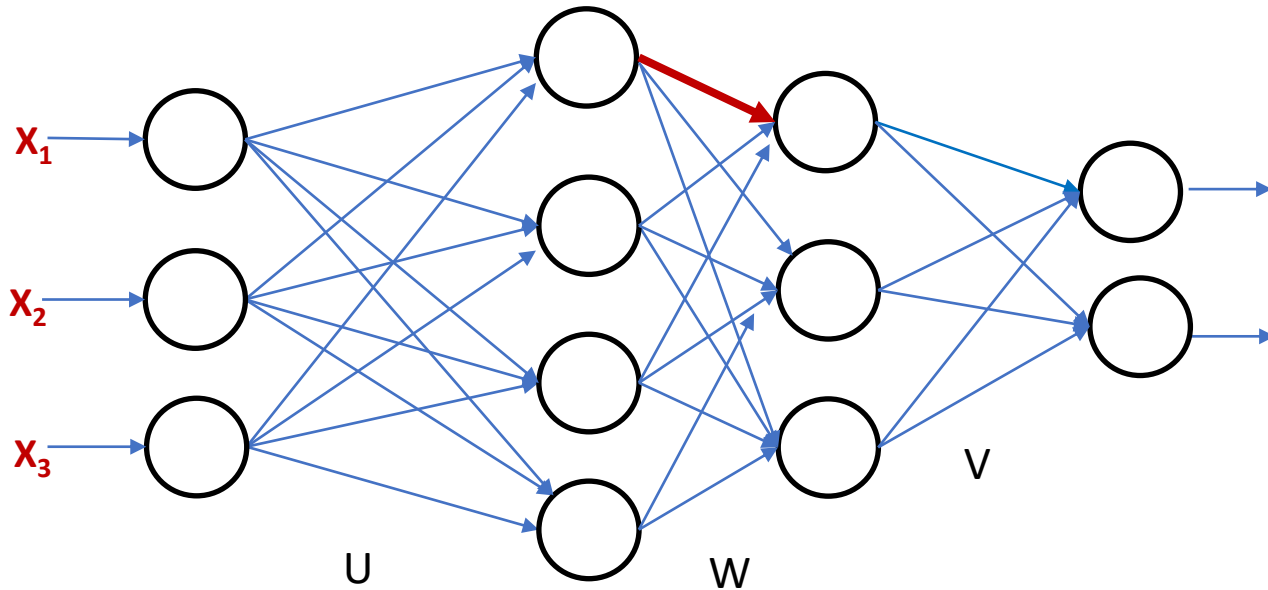


We may have multiple layers.

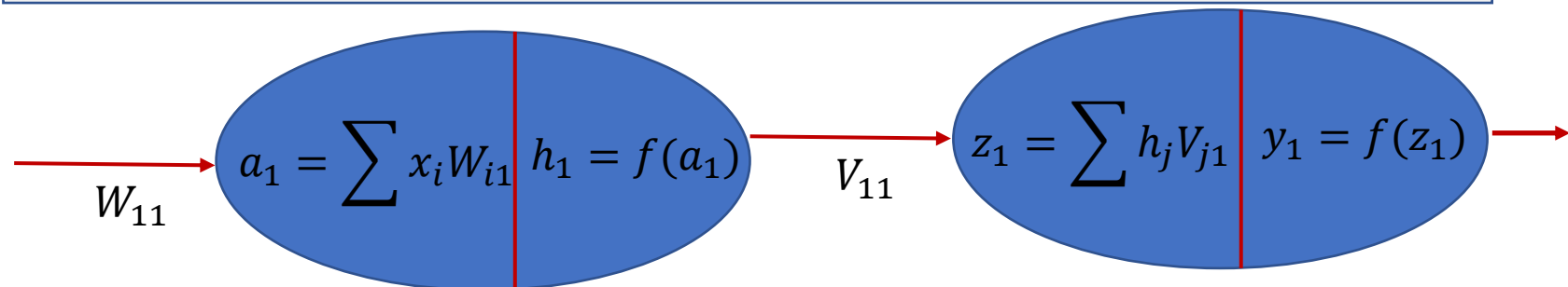


$$\frac{\delta E}{\delta V_{11}} = \frac{\delta z_1}{\delta V_{11}} \times \frac{\delta y_1}{\delta z_1} \times \frac{\delta E}{\delta y_1}$$

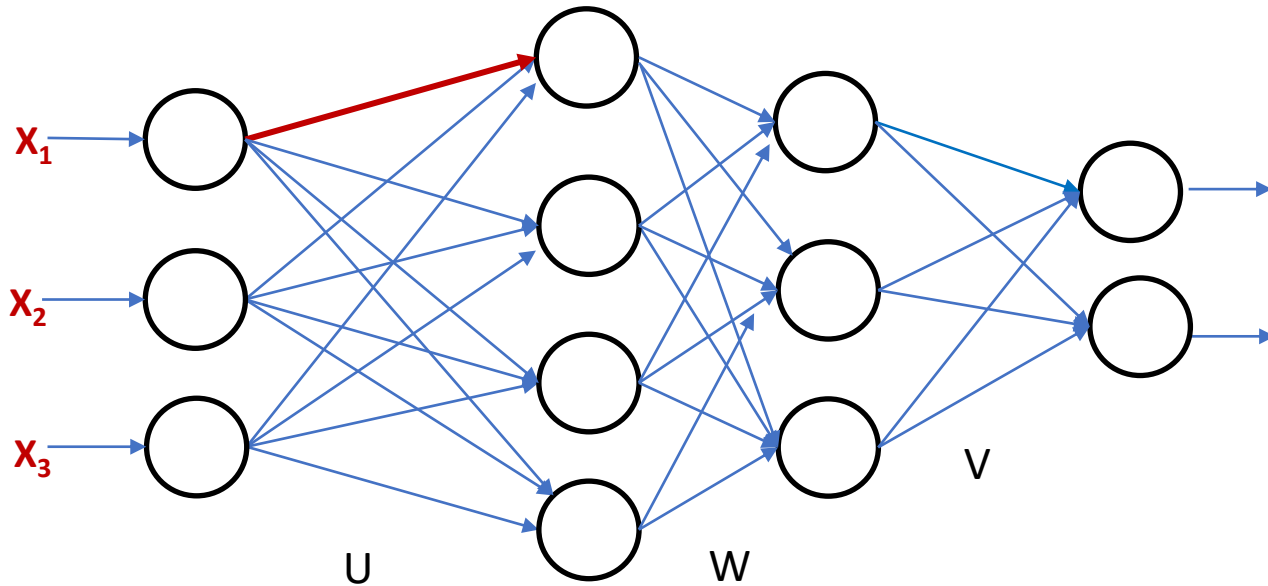
# We may have multiple layers



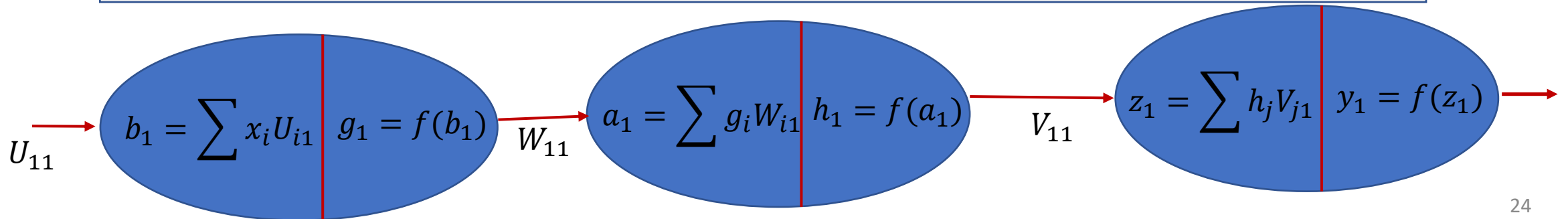
$$\frac{\delta E}{\delta W_{11}} = \frac{\delta a_1}{\delta W_{11}} \times \frac{\delta h_1}{\delta a_1} \times \frac{\delta z_1}{\delta h_1} \times \frac{\delta y_1}{\delta z_1} \times \frac{\delta E}{\delta y_1}$$



# We may have multiple layers



$$\frac{\delta E}{\delta U_{11}} = \frac{\delta b_1}{\delta U_{11}} \times \frac{\delta g_1}{\delta b_1} \times \frac{\delta a_1}{\delta g_1} \times \frac{\delta h_1}{\delta a_1} \times \frac{\delta z_1}{\delta h_1} \times \frac{\delta y_1}{\delta z_1} \times \frac{\delta E}{\delta y_1}$$





# Summary

- What is loss function?
- What are the parameters of a multilayer perceptron neural network?
- How to estimate parameters using backpropagation through time?